Homework set 1 — APPM5450, Spring 2017

From the textbook: 7.1, 7.3, 7.4. Optional: 7.2, 7.5.

Problem 1: Suppose that H is a Hilbert space, and that $(\psi_n)_{n=1}^{\infty}$ is an ON-set in H. Let \mathcal{P} denote the set of finite linear combinations of elements in $(\psi_n)_{n=1}^{\infty}$. Prove that:

 $(\psi_n)_{n=1}^{\infty}$ is a basis for $H \Leftrightarrow \mathcal{P}$ is dense in H.

Problem 2: Suppose that $f,g\in C(\mathbb{T})$. Prove that:

- (a) $f * g \in C(\mathbb{T})$.
- (b) f * g = g * f.